General Mathematics CSSA Trial HSC Examination 2005 Examination Mapping Grid

Section I

Question	Marks	Content	Syllabus	Targeted
			Outcomes	Performance
				Bands
1	1	DA3: Displaying Single Data Sets	P4	2-3
2	1	PB1: The Language of Chance	P9 P11	2-3
3	1	AM2: Modelling and Linear	P3 P5	2-3
		Relationships		
4	1	DA7: Correlation	H4	2-3
5	1	M6: Applications of Trigonometry	H1 H3	2-3
6	1	AM3: Algebraic Skills and Techniques	H2 H7	2-3
7	1	DA2: Data Collection and Sampling	P9	2-3
8	1	AM4: Modelling Linear and	H1 H2 H3 H5	3-4
		Non-Linear Relationships		
9	1	PB4: Applications of Probability	H7 H11	3-4
10	1	FM4: Credit and Borrowing	H1 H2 H5	3-4
11	1	M4: Right-angled Triangles	P2 P6	3-4
12	1	M3: Similarity of Two-Dimensional	P2 P6 P7	3-4
		Figures		
13	1	DA6: The Normal Distribution	H9	3-4
14	1	FM4: Credit and Borrowing	H2 H5 H8	3-4
15	1	M5: Further Applications of Area and	H1 H2 H6 H7	3-4
		Volume		
16	1	FM2: Investing Money	P2 P8	4-5
17	1	PB3: Multi-Stage Events	H7 H11	3-4
18	1	DA5: Interpreting Sets of Data	H4	3-4
19	1	FM4: Credit and Borrowing	H1 H2 H8	4-5
20	1	M5: Further Applications of Area and	H1 H2 H7	4-5
		Volume		
21	1	AM4: Modelling Linear and	H1 H2 H3	4-5
		Non-Linear Relationships		
22	1	FM5: Further Applications of Area	H2 H5 H8	4-5
		and Volume		
		Section II		

Section II

Question	Marks	Content	Syllabus Outcomes	Targeted Performance Bands
23 (a) (i)	1	DA5: Interpreting Sets of Data	H2	2-3
23 (a) (ii)		DA5: Interpreting Sets of Data	H4	3-4
23 (a) (iii)		DA5: Interpreting Sets of Data	H5	4-5
23 (b) (i)	2	M5: Further Applications of Area and Volume	H2 H3 H6 H7	3-4
23 (b) (ii)	1	M2: Applications of Area and Volume	P2 P6	2-3
23 (c) (i)	1	PB2: Relative Frequency and Probability	P2 P10	2-3
23 (c) (ii)	1	PB2: Relative Frequency and Probability	P2 P10	2-3

Question	Marks	Content	Syllabus	Targeted
			Outcomes	Performance
				Bands
23 (d) (i)	1	DA4: Summary Statistics	P2	2-3
23 (d) (ii)	1	DA4: Summary Statistics	P2	2-3
23 (e) (i)	1	M2: Applications of Area and Volume	P2 P6	3-4
23 (e) (ii)	2	M6: Applications of Trigonometry	H1 H2 H6 H7	3-4
24 (a)	2	PB3: Multi-Stage Events	H2 H3 H10	2-3
24 (b) (i)	2	AM3: Algebraic Skills and Techniques	H2 H7	3-4
24 (b) (ii)	2	AM3: Algebraic Skills and Techniques	H2 H7	3-4
24 (c) (i)	1	FM4: Credit and Borrowing	H2 H5 H8	2-3
24 (c) (ii)	1	FM4: Credit and Borrowing	H2 H5 H8	2-3
24 (c) (iii)	1	FM4: Credit and Borrowing	H2 H5 H8	3-4
24 (c) (iv)	2	FM4: Credit and Borrowing	H2 H5 H8	3-4
24(c)(v)	2	FM4: Credit and Borrowing	H2 H5 H8	4-5
25 (a) (i)	1	DA7: Correlation	H1 H2 H4	2-3
25 (a) (ii)	1	DA7: Correlation	H1 H5 H11	4-5
25 (b) (i)	1	FM3: Taxation	P2 P8	3-4
25 (b) (ii)	2	FM3: Taxation	P2 P8	3-4
25 (b) (iii)	1	FM3: Taxation	P2 P5 P8 P11	4-5
		AM2: Modelling and Linear		
		Relationships		
25(c)(i)	2	M4: Right-angled Triangles	P2 P3 P6 P7	2-3
25(c)(ii)	1	M4: Right-angled Triangles	P2 P3 P6 P7	2-3
25 (c) (iii)	2	M6: Applications of Trigonometry	H2 H6 H7	3-4
25 (d)	2	M1: Units of Measurement	P2 P7	3-4
26 (a) (i)	2	PB3: Multi-Stage Events	H2 H3 H4 H10	2-3
26 (a) (ii)	1	PB3: Multi-Stage Events	H2 H3 H4 H10	2-3
26 (a) (iii)	2	PB3: Multi-Stage Events	H2 H3 H4 H10	4-5
26(a)(iv)	1	PB3: Multi-Stage Events	H2 H3 H4 H10	4-5
26 (b)	2	DA3: Displaying Single Data Sets	P11	3-4
26(c)(i)	1	FM6: Applications of Trigonometry	H2 H5 H8	3-4
26(c)(ii)	2	FM6: Applications of Trigonometry	H2 H5 H8	3-4
26(c)(iii)	2	FM6: Applications of Trigonometry	H2 H5 H8 H11	4-5
27 (a)	2	AM1	P2	4-5
27 (b) (i)	2	DA6: The Normal Distribution	H9	4-5
27 (b) (ii)	1	DA6: The Normal Distribution	H9	4-5
27(c)(1)	1	DA5: Interpreting Sets of Data	H1 H4 H9	2-3
27(c)(ii)	1	DA5: Interpreting Sets of Data	HI H4 H9	3-4
27 (c) (iii)	3	DA5: Interpreting Sets of Data	H1 H4 H5 H9 H11	5-6
27 (d)	3	FM5: Further Applications of Area	H2 H5 H8	5-6
		and Volume		
28 (a) (i)	2	M7: Spherical Geometry	H1 H2 H7	4-5
28 (a) (ii)	2	M7: Spherical Geometry	H1 H2 H7	4-5
28 (a) (iii)	2	M1: Units of Measurement	P2	4-5
28 (b) (i)	2	AM4: Modelling Linear and	H1 H2 H3 H5	5-6
		Non-Linear Relationships	H11	
28 (b) (ii)	2	AM4: Modelling Linear and	H1 H2 H3 H5	4-5
		Non-Linear Relationships	H11	
28 (b) (iii)	2	AM4: Modelling Linear and	H1 H2 H3 H5	4-5
		Non-Linear Relationships	H11	
28 (b) (iv)	1	AM4: Modelling Linear and	H1 H2 H3 H5	4-5
		Non-Linear Relationships	H11	

General Mathematics CSSA Trial HSC Examination 2005 Examination Marking Guidelines

Section I

Q1	D	Q6 A	Q11 A	Q16 C	Q21 C
Q2	В	Q7 C	Q12 B	Q17 D	Q22 B
Q3	В	Q8 A	Q13 B	Q18 C	
Q4	D	Q9 B	Q14 B	Q19 C	
Q5	С	Q10 D	Q15 A	Q20 C	

Section II

Question	Solution	Criteria	Marks
23 (a) (i)	15	1 mark Correct answer	1
23 (a) (ii)	2000	1 mark Correct answer	1
23 (a) (iii)	Town 2 appears to be the safest as it has less cars stolen over the 5 year period. The area of the graph for town 2 appears to be smaller than the area for town 1.	1 mark Correct reason	1
23 (b) (i)	$A = \frac{h}{3}[d_f + 4d_m + d_l]$ = $\frac{5}{3}[0.8 + 4 \times 1.4 + 1.7]$ = 13.4 m ²	 2 marks Correct working and answer 1 mark Correct substitution in formula 	2
23 (b) (ii)	Volume = Ah = 13.5 × 6.5 = 87.75 $\approx 88 \text{ m}^3$	1 mark Correct answer	1
23 (c) (i)	$P(I) = \frac{2}{5}$	1 mark Correct answer	1
23 (c) (ii)	P has least chance of being selected as it only occurs once.	1 mark Correct answer	1
23 (d) (i)	Mean = 2.75	1 mark Correct answer	1
23 (d) (ii)	Standard Deviation ≈ 1.1	1 mark Correct answer	1
23 (e) (i)	$\angle DOA = (360 - 296) + 20 = 84^{\circ}$	1 mark Correct answer	1
23 (e) (ii)	Area = $\frac{1}{2}ab\sin C$ = $\frac{1}{2} \times 81 \times 75 \times \sin 84^{\circ}$ = 3021 m^2	 2 marks Correct answer 1 mark Correct substitution into formula 	2

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Question	Solution	Criteria	Marks
24 (a)	Number of ways	2 marks Correct answer and	2
	$= 4 \times 3 \times 2 \times 1$	explanation/justification	
	= 24	I mark Correct answer	
24 (b) (i)	$A = 4\pi r^2$	2 marks Correct rearrangement	2
	2 A	1 mark Significant progress toward	
	$r^{-} = \frac{1}{4\pi}$	s correct rearrangement	
	$r = \pm \sqrt{\frac{21}{4-1}}$		
24 (b) (ii)	ν 4π	2 manks Correct answer with 3	2
24 (0) (11)	$r = \sqrt{\frac{A}{A}}$	significant figures	2
	$V4\pi$	1 mark Correct answer without	
		rounding or correct substitution into	
	$=\sqrt{4\pi}$	formula	
	= 11.968268141		
	≈ 12.0		
24 (c) (i)	\$227963.68	1 mark Correct answer	1
24 (c) (ii)	Amount paid off	1 mark Correct answer	1
	= 230000 - 227963.68		
	= \$2036.32		_
24 (c) (iii)	Total amount paid	1 mark Correct answer	1
	$= 2240.80 \times 5$		
	= \$11204		-
24(c)(iv)	Interest charged	2 marks Correct answer	2
	= Prn	I mark Using correct principal or	
	$= 227963.68 \times \frac{0.096}{12} \times 1$	for using correct rate, but not both	
	- \$1822.71		
24(a)(y)	= \$1625.71	2 manks Correct answer	2
24(0)(0)	$2240.90 \times 19 \times 12$	1 mark Correct total amount with	2
	$= 2240.80 \times 18 \times 12$ = \$484012.80	subsequent error or correct interest	
	- \$404012.00	calculation with previous error	
	= 484012.80 - 230000	1	
	= \$254012.80		
25 (a) (i)	5 hours	1 mark Correct answer	1
25 (a) (ii)	Just because a person does less	1 mark Sensible statement	1
	homework does not imply they	explaining no causality	
	watch television, they may do many		
25 (b) (i)	ouner things as well.	1 mank Correct avaluation	1
23 (0) (1)	-59594 - 1630 - 430	I MARK Correct evaluation	
	= 57534		
25 (b) (ii)	Tax Payable	2 marks Correct answer	2
(-) ()	= 3762 + 0.38(57534 - 46000)	1 mark Selection of correct row of	_
	= \$8144.92	table and incorrect evaluation or	
		selection of incorrect row of table	
05 (1) (1)		but correct evaluation	
25 (b) (m)	The different gradients represent the	I mark Mentioning different tax	
	system	rates	
	system.		

Question	Solution	Criteria	Marks
25 (c) (i)	Final leg	2 marks Using Pythagoras'	2
	$=\sqrt{3.5^2+6.3^2}$	Theorem correctly and adding	
	= 7.2069	1 mark Attempt using Pythagoras'	
	Total distance $-7.2060 + 6.2 + 2.5$	Theorem	
	$= 7.2009 \pm 0.3 \pm 3.3$ = 17 0069		
	≈ 17 km		
25 (c) (ii)	$\tan X = \frac{3.5}{2}$	1 mark Correct tan ratio	1
	$\tan x = \frac{1}{6.3}$		
	$X \approx 29^{\circ}$		
25 (c) (iii)	Bearing from Start to Buoy 2	2 marks Correct answer	2
	= 100 - 29 - 71°	I mark Significant progress	
	- /1 Bearing from Buoy 2 to Finish	towards answer	
	= 71 + 180		
	= 251°		
25 (d)	Percentage Error	2 marks Correct answer	2
	$=\frac{20}{20}\times\frac{100}{20}$	1 mark Working towards correct	
	28000 1	answer	
$2(\langle z \rangle \langle z \rangle)$	= 0.0%		
26 (a) (1)	Correct tree diagram	2 marks Correct diagram including	2
		1 marks Any correct probabilities	
		on a branch	
26 (a) (ii)	$P(DD) = 0.2 \times 0.2 = 0.04$	1 mark Correct answer	1
26 (a) (iii)	P(at least 1 win)	2 marks Correct answer	2
	= 0.09 + 0.06 + 0.06 + 0.15 + 0.15	1 mark Significant progress toward	
26 (a) (iv)	= 0.51	s answer	1
$\frac{20(a)(1v)}{26(b)}$	P(100 wms) = 1 - 0.51 = 0.49	1 mark Correct answer	2
20(0)	it is then a stratified sample rather	1 mark Some statement regarding	2
	than a random sample	the sample type not being named	
		correctly	
26 (c) (i)	$S = V_0 (1 - r)^n$	1 mark Correct answer	1
	$= 2200(1-0.40)^{1}$		
	$= 2200 \times 0.60$		
	- \$1320		
26 (c) (ii)	$S = V_0 - Dn$	2 marks Correct answer	2
	0 = 2200 - 5D	1 mark Correct substitution into	_
	5D - 2200	formula	
	D = \$4400		
26 (c) (iii)	For declining balance method:	2 marks Correct answer with explan	2
2 ° (c) (iii)	Depreciation in 1st year	ation	_
	= 2200 - 1320	1 mark Correct answer with no	
	$\begin{bmatrix} = \$880 \\ Far a trial t 1 \\$	explanation or logical explanation	
	Por straight line method: Depreciation in 1st year	leading to incorrect answer	
	= \$440		
	Declining balance method is best to		
	use as it allows a higher tax		
	deduction.		

Question	Solution	Criteria	Marks
27 (a)	$\frac{3x+2}{x-1} - \frac{x-1}{x-1}$	2 marks Correct solution	2
	$\frac{-2}{2} = \frac{-3}{3} = 1$	1 mark Significant progress	
	3x + 2 $x - 1$ 3	towards correct answer	
	$\frac{1}{2} = \frac{1}{3} - \frac{1}{3}$		
	3x + 2 $x - 1 - 3$		
	$\frac{-2}{2} = \frac{-3}{3}$		
	3x + 2 $x - 4$		
	$\frac{333+2}{2} = \frac{33}{2}$		
	3(3x+2) = 2(x-4)		
	9x + 6 = 2x - 8		
	9x = 2x - 14		
	7x = -14		
	x = -2		
27 (b) (i)	<i>z</i> -score for Test 1:	2 marks Correct <i>z</i> -scores and	2
	$z = \frac{x - \bar{x}}{x - \bar{x}} = \frac{75 - 60}{-2} = 2$	conclusion	
	$\sigma^{-} - 7.5^{-} - 2$	1 mark Correct <i>z</i> -score calculation	
	<i>z</i> -score for Test 2:	method with no or incorrect	
	$x - \bar{x} - \bar{x} = 80 - 65 = 1$	conclusion	
	$z = \frac{\sigma}{\sigma} = \frac{15}{15} = 1$		
	Test 1 was the better mark as it has t		
	he higher <i>z</i> -score.		
27 (b) (ii)	Michelle's <i>z</i> -score in Test 2 was 1.	1 mark Correct answer	1
	Therefore 16% of students achieved		
	a mark higher than her.		
27 (c) (i)	Sonal	1 mark Correct answer	1
27 (c) (ii)	Interquartile range = 4	1 mark Correct answer	1
27 (c) (iii)	Any three valid comments	3 marks Three correct statements	3
		2 marks Two correct statements	
		1 marks One correct statements	

 $\frac{n}{\sqrt{range}} = \frac{1}{\sqrt{range}}$

Question	Solution	Criteria	Marks
27 (d)	$A = M \left[\frac{(1+r)^n - 1}{2} \right]$	3 marks Correct answer	3
		correct substitution	
	$0600 - 240 \left[(1 + 0.005)^n - 1 \right]$	1 mark Use of FV formula	
	$9600 = 240 \begin{bmatrix}$		
	$1.005^{n} - 1$		
	$9600 = 240 \left[\frac{0.005}{0.005} \right]$		
	$40 = \frac{1.005^n - 1}{100000000000000000000000000000000000$		
	0.005		
	$0.2 = 1.005^{n} - 1$	· · ·	
	1.2 = 1.005"		
	$1.005^{n} = 1.2$		
	n = 36.55539636		
	= 37 months		
	Using graphic calculator:		
	n = 0		
	PV = 0		
	PMT = 240		
	FV = -9600 P/V = 12		
	C/Y = 12		
	∴ 36.55539636 ≈ 37 months		
28 (a) (i)	8 am Friday in Sydney = 10 pm	2 marks Correct answer	2
	After 22 hour flight time in London	answer	
	is 8pm Friday		
28 (a) (ii)	Speed = $\frac{\text{Distance}}{1}$	2 marks Correct answer in knots	2
	Time	I mark Correct answer in km/h	
	$=\frac{17000}{22}$		
	= 772 727272 km/h		
	= 417.239348 knots		
	≈ 417 knots		
28 (a) (iii)	Let <i>x</i> be the amount of fuel used	2 marks Correct answer	2
	$\frac{x}{184} = \frac{184}{184}$	1 mark Correct ratio	
	$\begin{array}{cccccccccccccccccccccccccccccccccccc$		
	x = 177.93406593		
	≈ 178 tonnes		

Question	Solution	Criteria	Marks
28 (b) (i)	Let x be the length and y be the	2 marks Correct, logical argument	2
	width.	1 marks Significant progress	
	Perimeter = $x + y + x + y = 16$	towards solution	
	2x + 2y = 16		
	2(x+y) = 16		
	x + y = 8		
	y = 8 - x		
	Area $= lb$		
	=x(8-x)		
	$=8x-x^2$		
28 (b) (ii)	Values of areas:	2 marks Table copied and all areas	2
	0, 7, 12, 15, 16, 15, 12, 7, 0	correct	
28 (b) (:::)		1 mark Most areas correct)
20 (0) (111)	Area of Vegetable Patch	graph	2
	20	1 mark Correct graph without clear	
	e l	labels or with some incorrect points	
	bg 15		
	듚 10		
	d d		
	Area Area		
	0 2 4 6 8		
	Length of Fatch (m)		
28 (b) (iv)	From graph:	1 mark Correct answer	1
	Maximum area = 16 m^2		
	This occurs when $x = 4$.		
	So length and width must be 4 m.		
	$\mathbf{\wedge}$		
28 (b) (iv)	From graph: Maximum area = 16 m^2 This occurs when $x = 4$. So length and width must be 4 m.	I mark Correct answer	1